

# A Novel ANN Approach for Direct Microwave FET Noise Wave Parameter Extraction

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**Abstract**—The noise wave model provides relationships between the noise wave parameters and the noise parameters. However, since the noise wave model refers to the transistor intrinsic circuit, whose noise parameters are not directly measurable, the noise wave parameters are extracted based on the measured transistor noise parameters usually using time-consuming optimization procedures in circuit simulators. In this paper a new, faster and more efficient extraction approach based on artificial neural networks is proposed. The validation of the proposed approach is done in the case of the specific packaged HEMT based on AlGaAs/GaAs heterojunction by comparing the transistor noise parameters obtained using the extracted noise wave parameters with the measured noise parameters.

**Index Terms**—artificial neural network, FET, noise parameters, noise wave model, noise wave parameters.

## I. INTRODUCTION

Microwave FETs (MESFETs/HEMTs) are widely used in modern microwave communication systems as an integral part of low-noise communication devices. Therefore, over the years, many studies have been devoted to the characterization of these types of transistors in terms of the noise parameters ( $F_{min}$  – minimum noise figure,  $R_n$  – noise resistance and  $\Gamma_{opt}$  – optimum source reflection coefficient) and to their modeling [1-10]. A typical approach consists of using the equivalent-circuit representation with additional noise sources (voltage and/or current sources), as in the case of the Pospieszalski's noise model [6]. On the other hand, in recent years, the noise wave model treating the noise in terms of waves has appeared as a very appropriate noise model at the microwave frequencies [2], [7-9], [11-22]. The power of the wave representation of noise lies in its compatibility with the scattering matrix description of microwave networks. This is important because the scattering parameters used for performing the noise analysis are obtained with high accuracy by using vector network analyzers, which contribute to the accuracy of noise analysis [17].

The noise wave model is characterized by its parameters, called the noise wave temperatures, and provides the

relationships between these parameters and the noise parameters [2]. Nevertheless, as the noise wave model refers to the transistor intrinsic circuit, whose noise parameters are not directly measurable, direct analytical determination of the noise wave temperatures is not possible. For this reason, the extraction of these temperatures is done based on the measured transistor noise parameters usually using optimization procedures in circuit simulators. However, as it has already been shown earlier that the noise wave temperatures should be considered as frequency-dependent parameters to ensure the noise model accuracy [14], it is necessary to extract their values for each frequency separately. In that case, optimization procedures become time-consuming and quite inefficient extraction tool. Therefore, some more efficient extraction approach should be applied.

Artificial neural networks (ANNs) have proved to be a very powerful modeling tool for a range of problems in the field of microwaves, e.g. for the purpose of the transistor noise modeling [15], [20], [22-29]. This is primarily because ANNs have ability to learn from the presented data and to generalize (to give correct output for the input values that have not been used for the process of ANN training). Moreover, since ANN responses are based on performing basic mathematical operations and calculating elementary mathematical functions (such as an exponential or hyperbolic tangent function), they are obtained almost instantaneously.

In this paper, a new, faster and more efficient extraction approach based on ANNs is proposed. In addition to saving time, the proposed extraction approach also enables a very accurate transistor noise modeling using the noise wave model, which is demonstrated by applying the proposed extraction approach to the specific packaged HEMT based on AlGaAs/GaAs heterojunction.

The paper is organized as follows. After Introduction, Section II contains a short description of the noise wave model. The proposed extraction approach based on ANNs is presented in Section III. Section IV contains the most illustrative numerical results and obtained observations. Concluding remarks are given in Section V.

## II. NOISE WAVE MODEL OF MICROWAVE FETs

In the noise wave representation, the transistor intrinsic circuit, which is a noisy two-port network, is described by using a noiseless linear equivalent circuit with two additional noise wave sources at the input [2]. These noise wave sources are characterized by its parameters, called the noise wave

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temperatures - two real temperatures,  $T_a$  and  $T_b$ , and one complex correlation temperature,  $T_c = |T_c|e^{j\omega\tau_c}$ . These temperatures can be expressed in terms of the noise parameters of transistor intrinsic circuit - minimum noise figure,  $F_{min,i}$ , optimum source reflection coefficient,  $\Gamma_{opt,i} = |\Gamma_{opt,i}|e^{j\varphi_{opt,i}}$ , and noise resistance,  $R_{n,i}$ , as [2]:

$$T_a = T_0(F_{min,i} - 1) + \frac{4R_{n,i}T_0|\Gamma_{opt,i}|^2}{Z_0|1 + \Gamma_{opt,i}|^2}, \quad (1)$$

$$T_b = \frac{4R_{n,i}T_0}{Z_0|1 + \Gamma_{opt,i}|^2} - T_0(F_{min,i} - 1), \quad (2)$$

$$T_c = \frac{4R_{n,i}T_0\Gamma_{opt,i}}{Z_0|1 + \Gamma_{opt,i}|^2}, \quad (3)$$

where  $Z_0$  is the normalization impedance (50  $\Omega$ ) and  $T_0$  is the standard reference temperature (290 K).

### III. THE PROPOSED ANN APPROACH FOR MICROWAVE FET NOISE WAVE TEMPERATURE EXTRACTION

As already mentioned, since the noise wave model is related to the transistor intrinsic circuit, the noise wave temperatures are in relationships with the noise parameters of transistor intrinsic circuit, Eqs. (1-3) [2]. However, because the noise parameters of transistor intrinsic circuit are not directly measurable, direct analytical determination of these temperatures is not possible. Instead, the noise parameters of transistor intrinsic circuit can be replaced by the fully measurable transistor noise parameters in Eqs. (1-3), which leads to determination of the fictive noise wave temperatures,  $T_{af}$ ,  $T_{bf}$ ,  $|T_{cf}|$ , and  $\tau_{cf}$ . Compared to the noise wave temperatures that are related to the transistor intrinsic circuit, the fictive noise wave temperatures are related to the entire transistor. Although the fictive noise wave temperatures are irrelevant to the process of the transistor noise modeling, they can be very useful for the extraction of the noise wave temperatures [21]. Namely, as it has already been shown earlier, there is a strong correlation between the noise wave temperatures and the fictive noise wave temperatures [21]. Exactly this fact is used for development of a novel approach for efficient extraction of the noise wave temperatures, which enables avoiding time-consuming optimization procedures in circuit simulators.

The developed approach for extraction of the noise wave temperatures is based on ANN model presented in Fig. 1. The presented ANN is trained to determine the noise wave temperatures,  $T_a$ ,  $T_b$ ,  $|T_c|$ , and  $\tau_c$ , from the fictive noise wave temperatures,  $T_{af}$ ,  $T_{bf}$ ,  $|T_{cf}|$ , and  $\tau_{cf}$ , frequency,  $f$ , and ambient temperature,  $T$ . The presented ANN is based on a standard multilayer perceptron (MLP) structure [23] that consists of basic processing elements (neurons) grouped into layers: an

input layer, an output layer, as well as one/several hidden layers. In the case of MLP structure, each neuron is connected to all neurons from the adjacent layers, whereas there are no connections among neurons belonging to the same layer. Each neuron is characterized by a transfer function and each connection is weighted. The ANN learns relationship among sets of input–output data (training sets) by adjusting network connection weights and thresholds of activation functions. There are different algorithms for training of ANNs. The most frequently used are the backpropagation algorithm and its modifications with higher convergence order, as the Levenberg-Marquard algorithm [23].

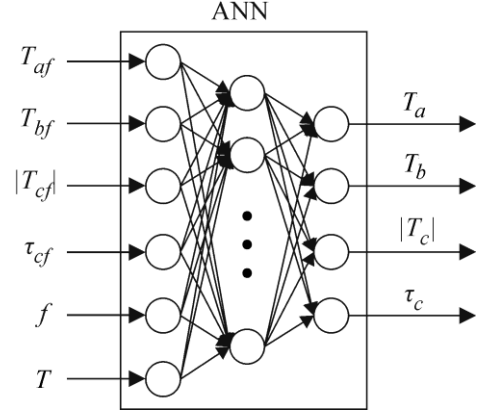


Fig. 1. The proposed ANN model for extraction of the noise wave temperatures.

The procedure of ANN training and validation is illustrated in the flowchart given in Fig. 2 and can be described as follows:

1. Design the small-signal equivalent circuit schematic of the considered transistor within the standard circuit simulator and implement the noise wave model expressions,
2. Generate  $R$  and  $L$  ( $L \geq 0.1R$ ) random samples of  $F_{min,i}$ ,  $R_{n,i}$ ,  $|\Gamma_{opt,i}|$ ,  $\varphi_{opt,i}$ ,  $f$  and  $T$ ,
3. For each of  $R$  and  $L$  samples of  $F_{min,i}$ ,  $R_{n,i}$ ,  $|\Gamma_{opt,i}|$ , and  $\varphi_{opt,i}$  calculate  $T_a$ ,  $T_b$ ,  $|T_c|$ , and  $\tau_c$ , using Eqs. (1-3),
4. For  $R$  and  $L$  different combinations of calculated values of  $T_a$ ,  $T_b$ ,  $|T_c|$ , and  $\tau_c$ , and randomly sampled values of  $f$  and  $T$ , simulate the noise parameters of entire transistor,  $F_{min}$ ,  $R_n$ ,  $|\Gamma_{opt}|$ , and  $\varphi_{opt}$ , by using the noise wave model implemented within the standard circuit simulator in step 1,
5. Apply the Eqs. (1-3) to the simulated values of  $F_{min}$ ,  $R_n$ ,  $|\Gamma_{opt}|$ , and  $\varphi_{opt}$ , and calculate  $T_{af}$ ,  $T_{bf}$ ,  $|T_{cf}|$ , and  $\tau_{cf}$ ,
6. Build the training set ( $R$  samples) and validation test set ( $L$  samples), where the inputs are  $T_{af}$ ,  $T_{bf}$ ,  $|T_{cf}|$ ,  $\tau_{cf}$ ,  $f$  and  $T$ , and outputs are  $T_a$ ,  $T_b$ ,  $|T_c|$ , and  $\tau_c$ ,
7. Train a certain number of ANNs with one hidden layer and different number of hidden neurons,
8. Validate ANNs by comparing ANN response with the reference values not used for the network training (validation test set with  $L$  samples),

9. If the test results do not have satisfactory accuracy, increase  $R$  and repeat steps 2-8. Otherwise, proceed to the next step,
10. Choose ANN showing the best statistics. That network is further used for the extraction of the noise wave temperatures.

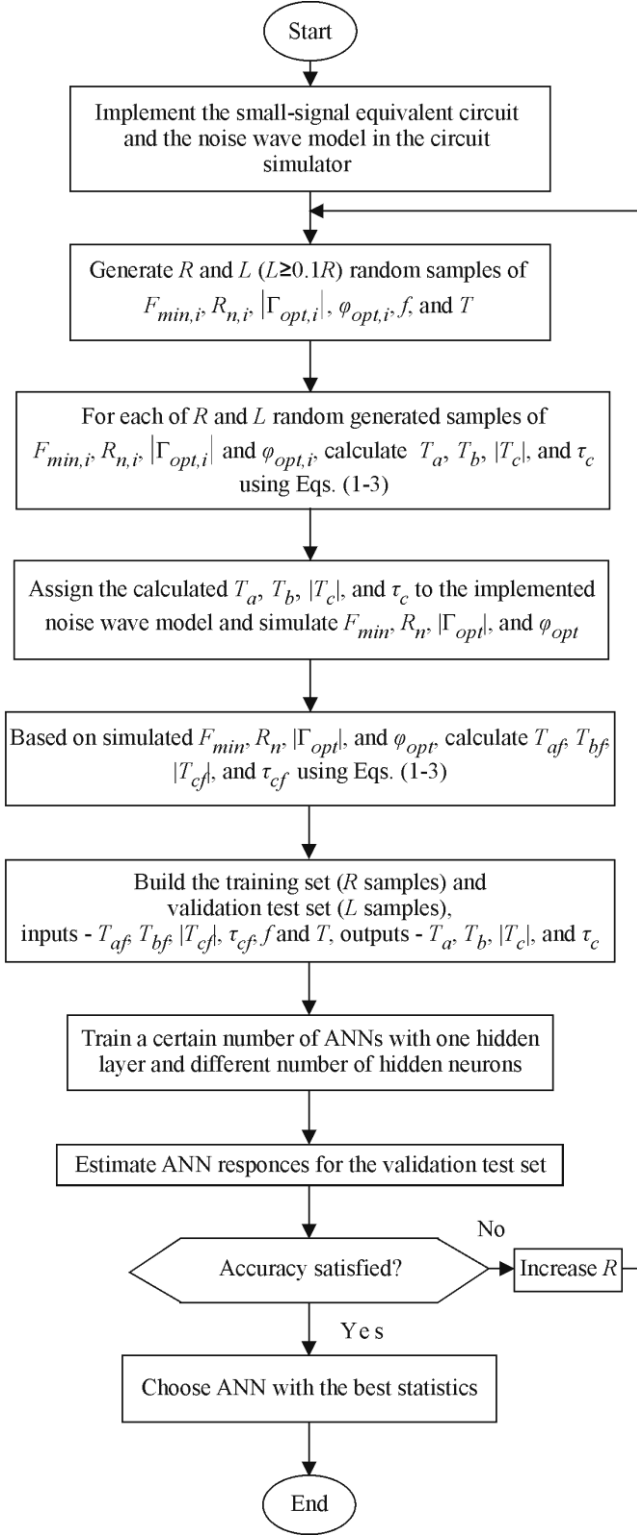


Fig. 2. Flowchart illustrating the training procedure of ANNs that are used for extraction of the noise wave temperatures.

#### IV. NUMERICAL RESULTS AND DISCUSSION

In order to validate the presented ANN approach for extraction of the noise wave temperatures, it was applied to a packaged HEMT based on AlGaAs/GaAs heterojunction, type NE20283A by NEC. In the case of the considered transistor, the  $S$  parameters were measured by using a vector network analyzer, whereas the noise parameters were obtained from the noise figure measured in input matched conditions, F50 [30]. They were available in the frequency range 6-18 GHz over the temperature range 233-333 K, 20 K step.

The equivalent circuit of a packaged HEMT, which was used for validation of the presented ANN extraction approach, is shown in Fig. 3 [30]. It consists of intrinsic and extrinsic parts. The intrinsic circuit is common to the most of microwave FET models, and it is denoted by the dashed line. Parasitic effects and the package are represented by the remaining extrinsic elements embedded in the circuit.

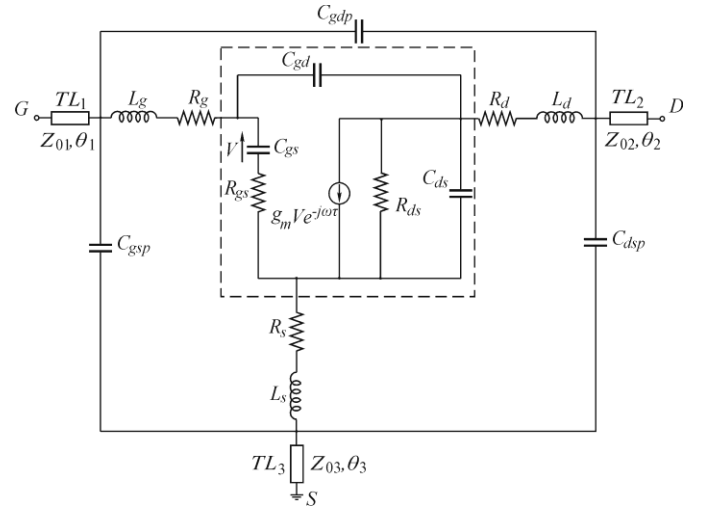


Fig. 3. Equivalent circuit of HEMT in packaged form.

As can be seen in Fig. 3, there are 19 equivalent circuit elements. The values of small-signal equivalent circuit elements of the considered transistor were taken from [30].

First, the values of the noise parameters of transistor intrinsic circuit were generated randomly. Then, the noise wave temperatures determined from these random generated noise parameters of transistor intrinsic circuit were used to obtain the fictive noise wave temperatures within ADS [31] circuit simulator. After that, the appropriate training and validation test sets with a certain number of samples were built. By using the built training set and the Levenberg-Marquard algorithm [23], several ANNs with one hidden layer and different number of hidden neurons were trained within MATLAB [32] software environment. To estimate the accuracy of the ANN learning and generalization, the trained ANNs were tested on the built training and validation test sets, respectively, by using the following metrics: average test error (ATE), worst case error (WCE), and Pearson product-moment correlation coefficient ( $r$ ) [23]. It should be mentioned that the number of samples within the training set was gradually increased and the process of ANN training was repeated until

the network with the best performance was obtained. Among the trained ANNs, ANN with the highest accuracy has one hidden layer, with five neurons. This ANN was trained with the training set contained 329 samples, whereas the validation test set contained 37 samples. The test statistics on training and validation test set for the chosen ANN is given in Table I.

TABLE I  
TEST STATISTICS FOR THE CHOSEN ANN

	ATE (%)	WCE (%)	$r$
<i>Training set</i>			
$T_a$	0.1238	0.5509	0.999970149
$T_b$	0.1021	0.4989	0.999981464
$ T_c $	0.0904	0.4473	0.999985470
$\tau_c$	0.1618	0.8713	0.999968505
<i>Validation test set</i>			
$T_a$	0.1595	0.4529	0.999968256
$T_b$	0.1197	0.5843	0.999978037
$ T_c $	0.1141	0.5185	0.999981384
$\tau_c$	0.1697	0.7527	0.999972099

The proposed ANN was used for determination of the noise wave temperatures in the whole temperature and frequency range. In order to validate the presented ANN based extraction approach, the determined noise wave temperatures were assigned to the noise wave model implemented within ADS [31], and the transistor noise parameters were simulated. The simulated noise parameters were compared with the corresponding measured data.

As an illustration, Figs. 4 and 5 present the simulated  $F_{min}$ ,  $R_n$ , and  $\Gamma_{opt}$  and the corresponding measured data. The results shown in Figs. 4 and 5 were obtained for the ambient temperatures of 233 K and 253 K, respectively, in the frequency range from 6 to 18 GHz. It can be seen that the simulated values of noise parameters are very close to the measured ones, confirming the accuracy of the proposed extraction approach.

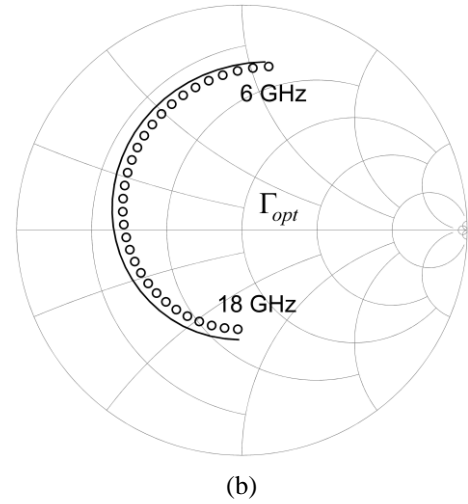
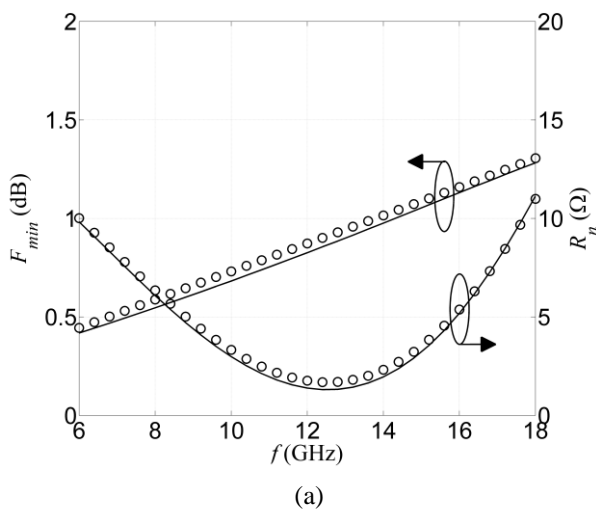


Fig. 4. Measured (symbols) and simulated (lines) values of: (a)  $F_{min}$  and  $R_n$ , (b)  $\Gamma_{opt}$ , depending on the frequency at 233 K.

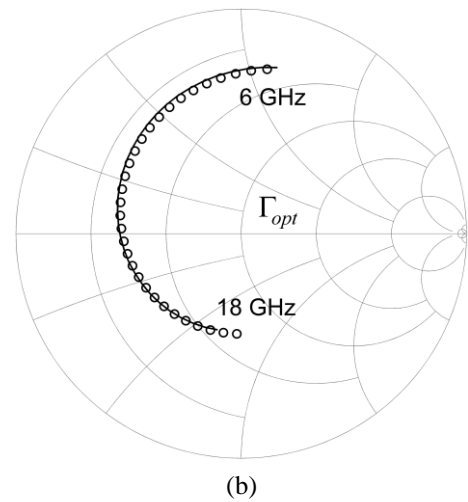
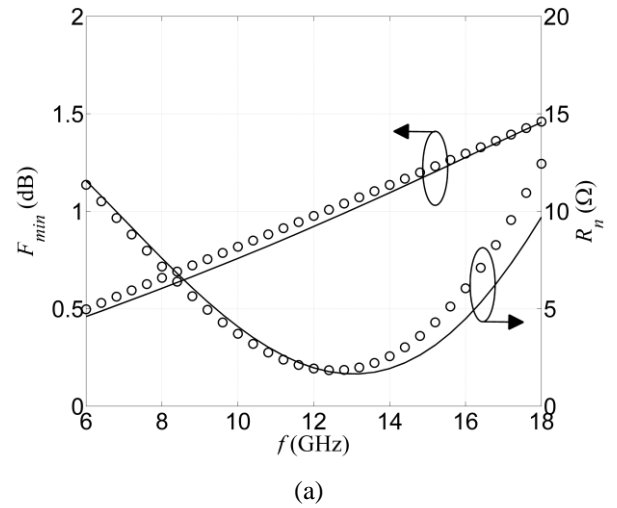


Fig. 5. Measured (symbols) and simulated (lines) values of: (a)  $F_{min}$  and  $R_n$ , (b)  $\Gamma_{opt}$ , depending on the frequency at 253 K.

## V. CONCLUSION

The noise wave temperatures are extracted based on the measured transistor noise parameters usually using optimization procedures within microwave circuit simulators. As the noise wave temperatures are frequency dependent parameters, the optimization procedures used for their extraction are time-consuming. In this paper, the more efficient extraction approach based on ANNs is presented. Namely, ANN is trained to determine the noise wave temperatures based on the fictive noise wave temperatures, frequency and ambient temperature.

With the aim to validate the proposed extraction approach, it was applied to a specific packaged HEMT over wide temperature range. The corresponding noise parameters of entire transistor circuit were simulated in the circuit simulator based on the obtained noise wave temperatures. A good agreement between the simulated and the measured transistor noise parameters proves validity of the proposed extraction approach.

## ACKNOWLEDGMENT

The work was supported by the TR-32052 Project of the Serbian Ministry of Education, Science and Technological Development. The authors would like to thank prof. Alina Caddemi, University of Messina, Italy, for providing the measured data.

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